

# Preparation of Nanostructures (Příprava Nanostruktur)

Jaroslav Hamrle

jaroslav.hamrle@vsb.cz

December 16, 2014

# Outline

- 1 **Content**
- 2 Relation between symmetry of crystals and crystal properties
- 3 Introduction
- 4 Bulk crystal growth
- 5 Thin film preparation
- 6 Lateral structures
- 7 ATR / Surface plasma resonance

## Překrytí obsahu přednášky s jinými předměty:

- MBE, napařování (sputtering) → Hlubina (vakuová fyzika)
- absorpce, desorpce molekul na površích → Hlubina (vakuová fyzika)
- tenké vrstvy (napařování, sputtering, CVD) → Postava
- techniky studia tenkých vrstev (XRD, SEM, AFM, RHEED, LEED) → jiné předměty

# Vyučující (2014-2015)

## Vyučující (2014-2015)

- Jaroslav Hamrle
- Rudolf Sýkora
- Illa Ramakanth
- Radek Ješko

# Nabízený obsah přednášky:

## IIIa Ramakanth (3 lessons)

- ① Chemical deposition methods for the formation of thin films
  - Chemical approach (preparation)
  - Chemical Vapor Deposition (CVD) process (chemical method)
  - Electrodeposition and solid phase method (chemical method)
  - Co-precipitation approach (chemical method)
  - Sol-gel (chemical method)
  - Hydrothermal synthesis / Solvothermal method (chemical method)
  - Ultrasonic assisted wet chemical route
  - Spin coating (chemical method)
  - Lithography
- ② Fullerenes: Structure, Preparation, Properties & applications
- ③ Carbon Nanotubes: Structure, Preparation, Properties & applications

# Nabízený obsah přednášky:

## Rudolf Sýkora

- krystalografie, 2D krystalografie, pocítání vzdalenosti rovin
- relaxace povrchu,
- elektronova struktura povrchu (kap 2 ze surface science)
- kap. 8. + 9.rekonstrukce povrchu; atomova struktura povrchu
- kap. 11. elektronova struktura povrchu

## Radek Ješko

- fyzikální depozice: MBE, naprašování (sputtering) [bude upřesněno]

# Nabízený obsah přednášky:

## Jaroslav Hamrle

- symetrie krystalů a jejich vliv na vlastnosti materiálů
- absorpce, desorpce, teorie růstů krystalů a tenkých vrstev (?)
- charakterizační techniky podle zájmu (např. NMR, surface plasmons a ATR, MOKE ?)

# Praktikum z pokročilých technologií

Dvě možnosti jak proběhne praktikum:

- 1 exkurze nebo
- 2 příprava a charakterizace feritů:
  - např.  $\text{CrFe}_2\text{O}_4$ ,  $\text{ZnFe}_2\text{O}_4$ ,  $\text{CuFe}_2\text{O}_4$ ,  $\text{NiFe}_2\text{O}_4$ ,  $\text{BiFeO}_3$
  - 8 vzorků (2 tloušťky, 4 žíhací teploty), připraveno pomocí dipping
  - charakterizace: XRD, VSM, AFM (případně SEM), případně elipsometrie a magento-optická spektroskopie, případně XPS
  - reálná šance opublikovat výsledky (nyní studujeme podobnou sadu vzorků)



# Outline

- 1 Content
- 2 Relation between symmetry of crystals and crystal properties
- 3 Introduction
- 4 Bulk crystal growth
- 5 Thin film preparation
- 6 Lateral structures
- 7 ATR / Surface plasma resonance

# Outline

- 1 Content
- 2 Relation between symmetry of crystals and crystal properties
- 3 Introduction**
- 4 Bulk crystal growth
- 5 Thin film preparation
- 6 Lateral structures
- 7 ATR / Surface plasma resonance

# Type of structures

## Types of structures

- bulks (including bulk superstructures)
- layers
- 2D structures (lithography, self-organizing growth)
- 3D structures (special lithography, 3D printing)

# Basic material structures

## Basic material structures from material point of view:

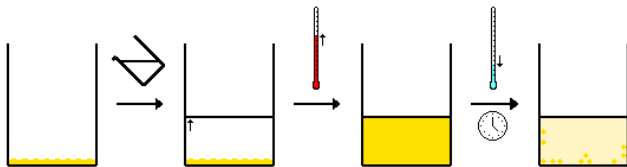
- single crystal (also known as monocrystals or epitaxial)
- polycrystals (small single crystals randomly oriented)
- amorphous (e.g. glass)

# Outline

- 1 Content
- 2 Relation between symmetry of crystals and crystal properties
- 3 Introduction
- 4 Bulk crystal growth
- 5 Thin film preparation
- 6 Lateral structures
- 7 ATR / Surface plasma resonance

# Crystal growth techniques I: using one solvent

- slow cooling of the solvent (*rozpouštědlo*): substances that are much more soluble in a solvent at high temperature than at low temperature



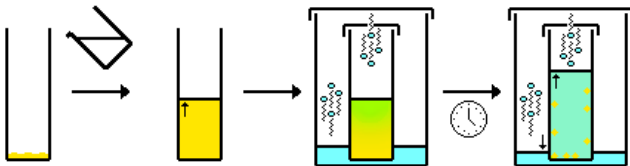
- slow evaporation of the solvent [solvent evaporates → crystal growth]
- solvent can be also liquid metal (e.g. Sn-tin)

[http://en.wikipedia.org/wiki/Recrystallization\\_\(chemistry\)](http://en.wikipedia.org/wiki/Recrystallization_(chemistry))

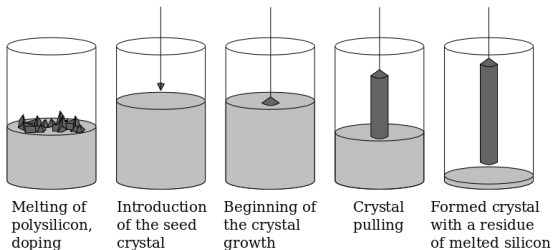
# Crystal growth techniques I: using two solvents

Two solvents (substances that are very soluble in one solvent and insoluble in a second solvent. The two solvents must be miscible, i.e. soluble in each other in all proportions):

- two solvent evaporation [dissolve substance in good solvent → add bad solvent → good solvent evaporates → crystal growth in bad solvent]
- two solvent liquid diffusion [dissolve substance in good solvent → add bad solvent → crystal growth in mixture of bad and good solvent].
- two solvent vapour diffusion [dissolve substance in good solvent → add bad solvent to surrounding → bad solvent mixes with good through diffusion of vapours → crystal growth in bad solvent]



# Crystal growth techniques II: Czochralski process

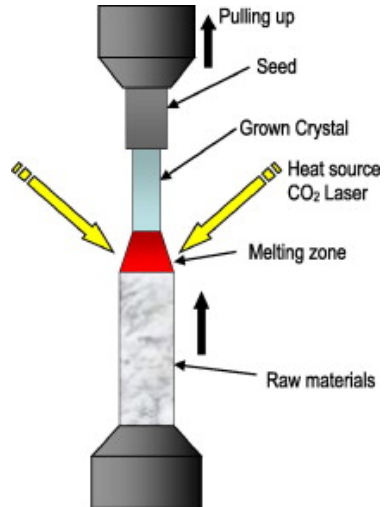


- high quality crystal growth of single crystals, to very large size (length 1-2 m, industrial diameter for wafers upto 450 mm)
- semiconductors (e.g. Si, Ge, GaAs), metals (e.g. Pd, Pt, Ag, Au), salts, etc.
- defects later removed by subsequent zone recrystallization.



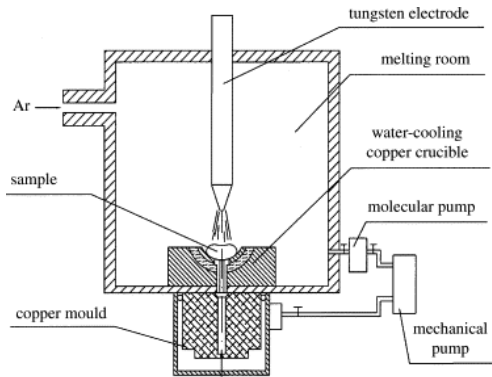
# Crystal growth techniques III: Laser Heated Pedestal Growth (LHPG)

- similar to Czochralski process, but no crucible needed
- heating by power laser
- high purity and low stress crystals
- allows to growth materials with very high melting points
- when heating starts with single crystal on top, can produce single crystal



# Polycrystal growth: arc melting/remelting

- melting or remelting in weak vacuum (usually Ar residual atmosphere)
- creation of metal polycrystals, with defined composition
- allows to melt small amounts of materials
- vacuum remelting and slow cooling: removal of residual gas and high vapour pressure elements (C,S,O,Mg), larger crystal size, stable structure obtained.



Huag et al, Materials Science and Engineering: A 422, 309, (2006)

# Crystal growth: nucleation

## 1. Crystal nucleation:

- small particle of crystal is created (nucleated), with random crystallographic orientation.
- homogenous/heterogenous (without/with influence of the external particle).
- nucleus appears slowly (then crystal may growth quickly).
- external crystal can be used as a seed.

# Crystal growth: growth

## 2. Crystal growth:

- In ideal case, crystal grows layer by layer added to the nucleated seed. The interface between crystal and vapour/solvent is atomically sharp.
- Non-uniform lateral growth: The surface advances by the lateral motion of steps which are one interplanar spacing in height.
- Uniform lateral growth: The surface advances normal to itself without the necessity of a stepwise growth mechanism.

# Outline

- 1 Content
- 2 Relation between symmetry of crystals and crystal properties
- 3 Introduction
- 4 Bulk crystal growth
- 5 **Thin film preparation**
- 6 Lateral structures
- 7 ATR / Surface plasma resonance

# Thin film preparation

## Techniques of thin film preparation

- physical techniques (usually physical vapour deposition, differing by source of vapour (MBE, sputtering, ion plating))
- chemical techniques (spin coating, chemical solution deposition (sol-gel), chemical vapour deposition)

# Physical deposition techniques: physical vapour deposition (PVD)

PVD involves: **Vapour formation** → **vapour transformation** → **film formation**

Vapour phase creation:

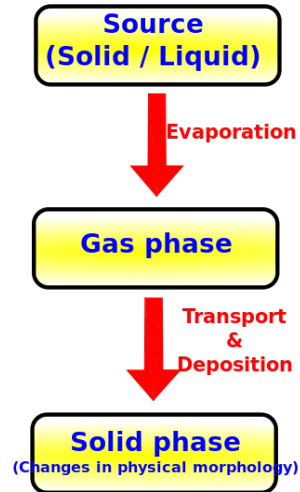
- evaporation
- sputtering
- ion plating

Vapour transportation:

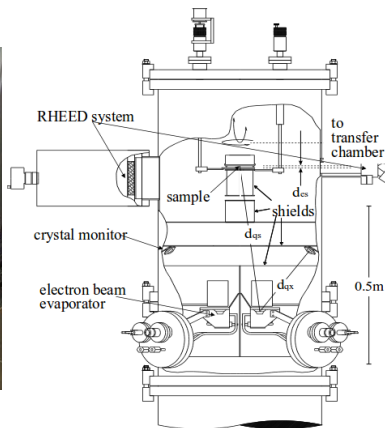
- collisions (can be related with cluster formation)
- ionizations

Condensation on substrate:

- nucleation, growth, ion bombardment, redeposition etc.

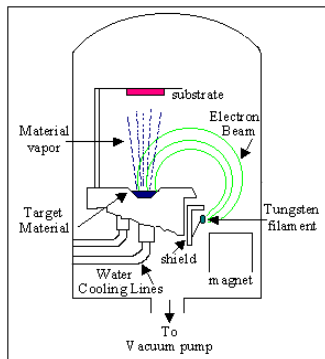


# Example of molecular beam epitaxy, (M.Jourdan, Mainz)



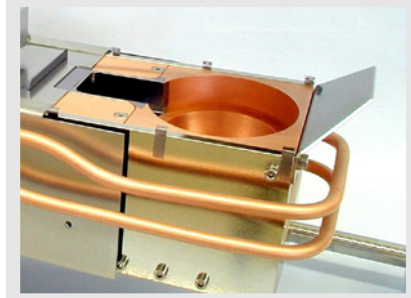
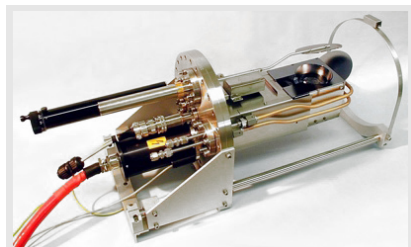


# Sources of vapours I: electron beam evaporators



Local heating by electron bombardment → evaporation of the target material → clean deposition of the target

[www.mbe-components.com](http://www.mbe-components.com)

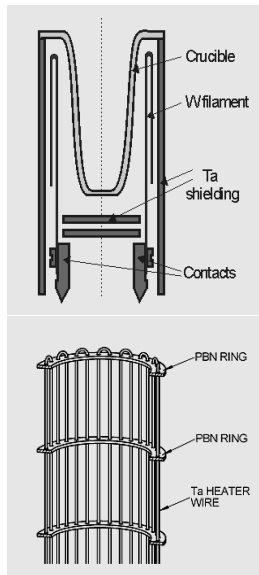


# Source of vapours II: Effusion cells (Knudsen Cell)

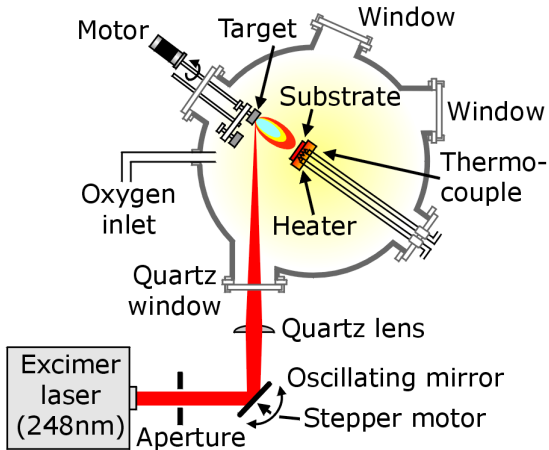


Thermal evaporation out of a heated crucible ( $T_{\max} \approx 1800^{\circ}\text{C}$ )

[www.mbe-components.com](http://www.mbe-components.com)



# Source of vapour III: Pulse laser deposition (PLD)



Problem of PLD: droplets ( $\mu\text{m}$ -sized balls deposited together with vapour).

<http://www.egr.msu.edu/>

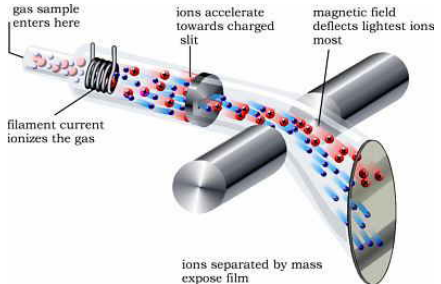
# Control of the deposition

## Deposited thickness gauge

Oscillating Crystal Monitor  
[change of mass  $\rightarrow$  change of resonance frequency]



## Mass Spectrometer

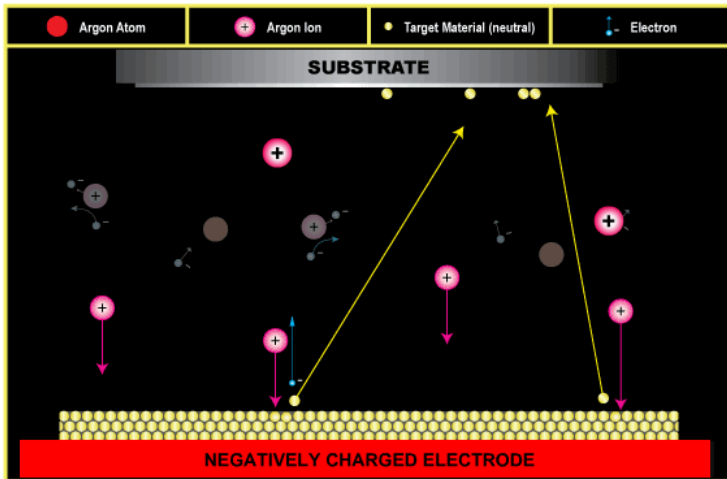


# Sputtering

## Sputtering:

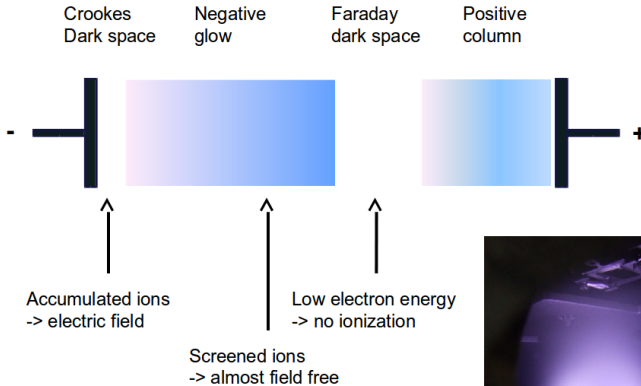
- ejection of atoms from target due to bombardment of energetic particles ( $E \gg 1 \text{ eV}$ ).
- commonly use for thin-film deposition, etching or analytical material study.
  - 1 create plasma (dc, rf, mw)
  - 2 plasma loses energy to surroundings (bombardment)
  - 3 for plasma, atoms of noble gas of similar weight as target is used (e.g. Ar for 3d metals)

# dc-sputtering

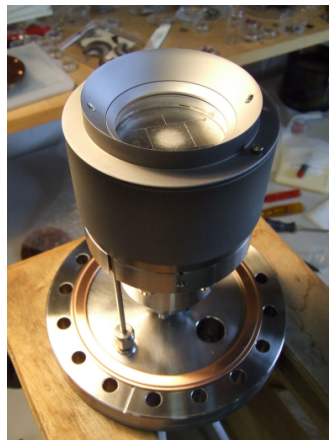
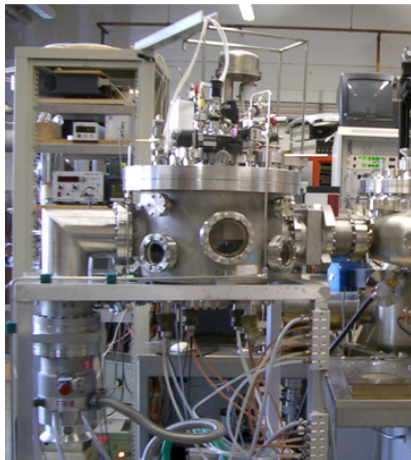


<http://www.ajaint.com/whatis.htm>

# dc-sputtering: Glow Discharge



# Sputtering: example



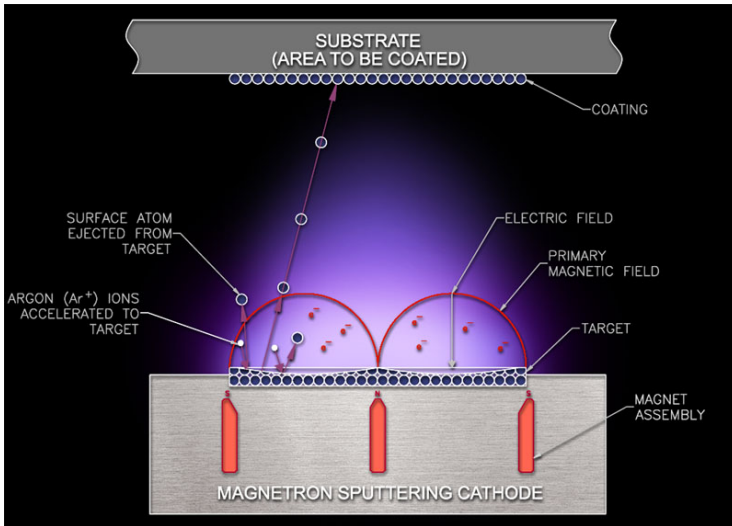


# Sputtering: industrial sputtering of glass



**Figure 1:** Horizontal inline sputter coater for architectural glass; annual throughput up to 8,000,000 m<sup>2</sup>

# Sputtering: magnetron

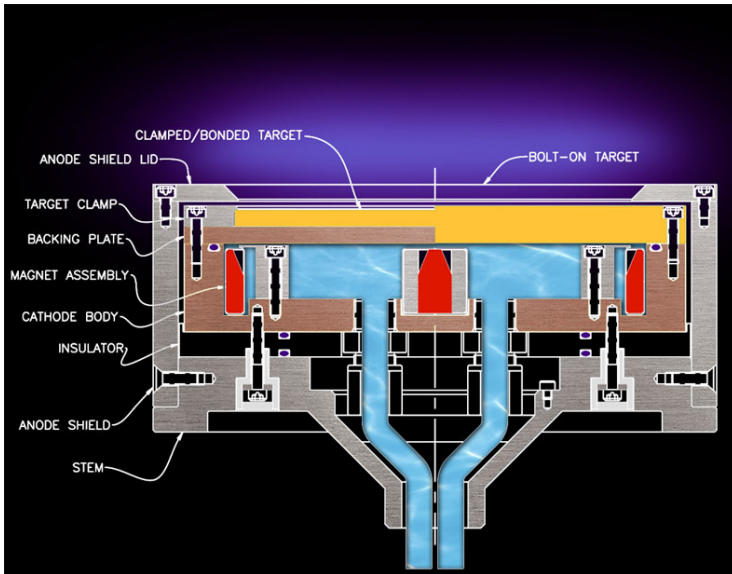


# Sputtering: magnetron

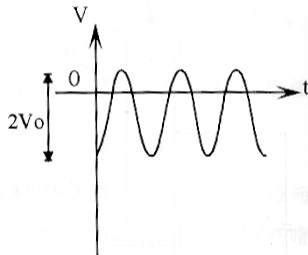
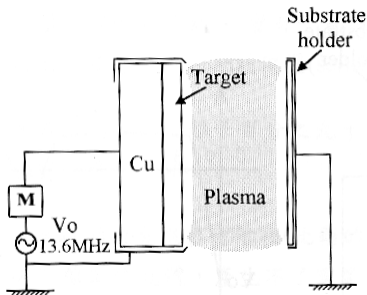
## Added magnetic field drives free electrons:

- electrons do not touch the target, and hence do not heat it
- electrons are localized above the target, and hence enhancing probability of ionization of noble gas  $\Rightarrow$  increases deposition rates
- recombination of free electrons and ions  $\Rightarrow$  glowing plasma

# Sputtering: magnetron



# Sputtering: rf sputtering



- Plasma is generated by radio-frequency (rf) field (MHz).
- Rf-sputtering avoids charge build-up on insulating targets (e.g. allows to sputter oxides).

# Ion plating

Atoms of target are ionized, to increase their speed prior the deposition → atom can penetrate deeper into the substrate

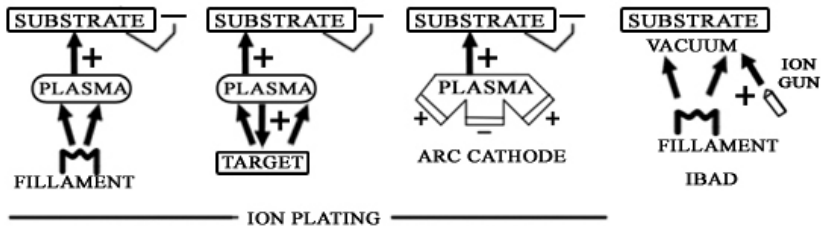
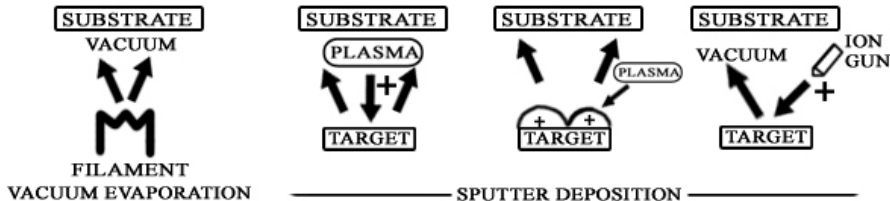
**Goal (1):** placement of atoms into substrate:

- gold plating
- steel hardening (e.g. layer of TiN)

**Goal (2):** crystal defects caused by atom irradiation:

- interface roughness control (magnetization anisotropy control)
- defects in AFM/FM interface ⇒ exchange bias control
- ...

# PVD techniques - comparison



<http://www.eclatcoating.com/learn/pvdcoating.php>

# Chemical deposition

- Involves chemical change at a solid surface
- Unidirectional deposition
  - electroplating (Although very cheap, very high quality Au/Co layers with atomically sharp interface has been demonstrated.)
  - chemical solution deposition (CSD), or sol-gel (transformation of colloidal solution (sol) into solid layer (gel))
  - spin-coating: liquid precursor is spread on a thin plate by spinning.
  - chemical vapour deposition (CVD): gas precursor.
  - dip coating
  - electrospray deposition



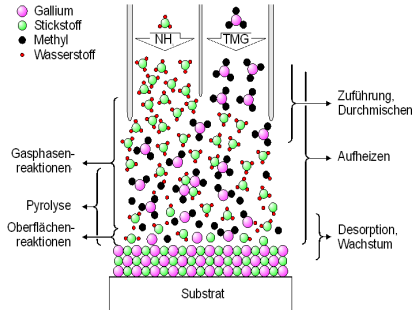
# Chemical vapour deposition (CVD)

- Film components bound in gas molecules
- Gas molecules directed on heated substrate
- Chemical reaction creates film material
- Gaseous by-products

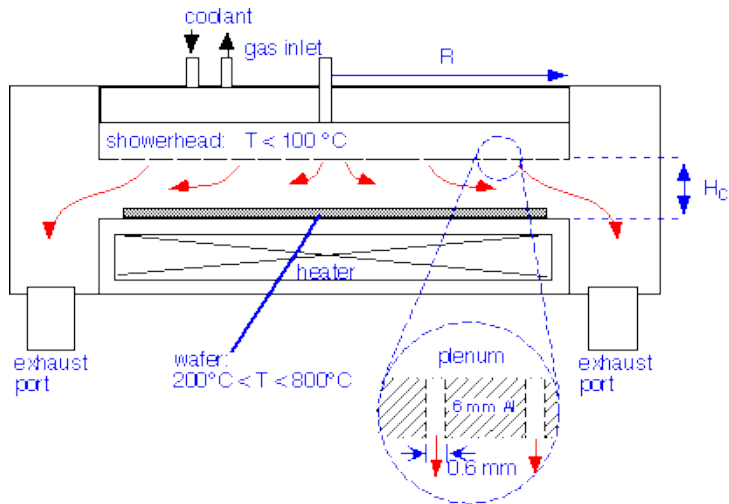


[http://thermodynamik.uni-duisburg.de/mitarbeiter/atakan/cvd\\_intro.htm](http://thermodynamik.uni-duisburg.de/mitarbeiter/atakan/cvd_intro.htm)

## GaN deposition ( $\text{NH}_3 + \text{TriMethylGalium}$ )



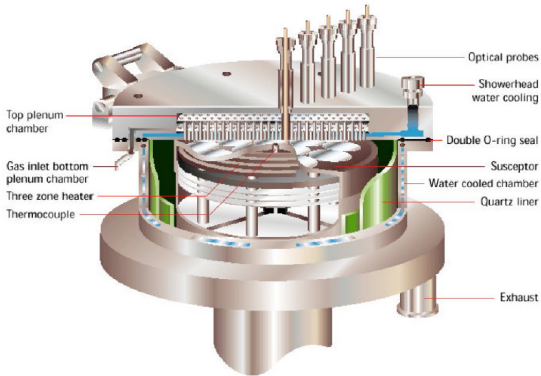
## CVD - reactors



<http://www.timedomaincvd.com>

# gallium nitride – industrial CVD reactor

## The C(lose) C(ouple) S(hower) Head reactor



Close Coupled Showerhead

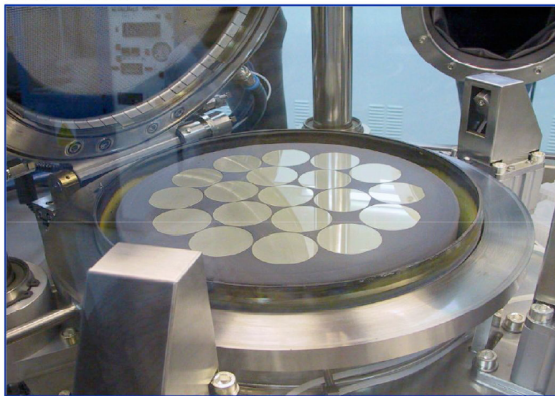
Date: 23.07.2004-16

Thomas Swan Scientific Equipment

RIXTRON

# gallium nitride – industrial CVD reactor

19x2" CCS Reactor



Close Coupled Showerhead

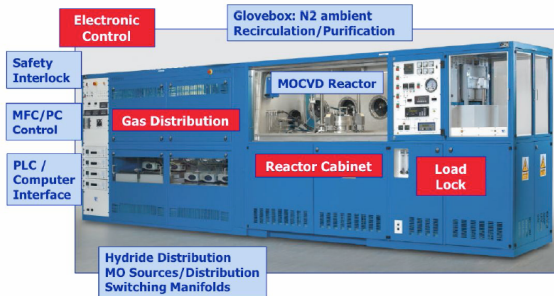
TRIS P  
26.07.2004 51

Thomas Swan  
Scientific Equipment

RIXTRON

# gallium nitride – industrial CVD reactor

## CCS MOCVD System



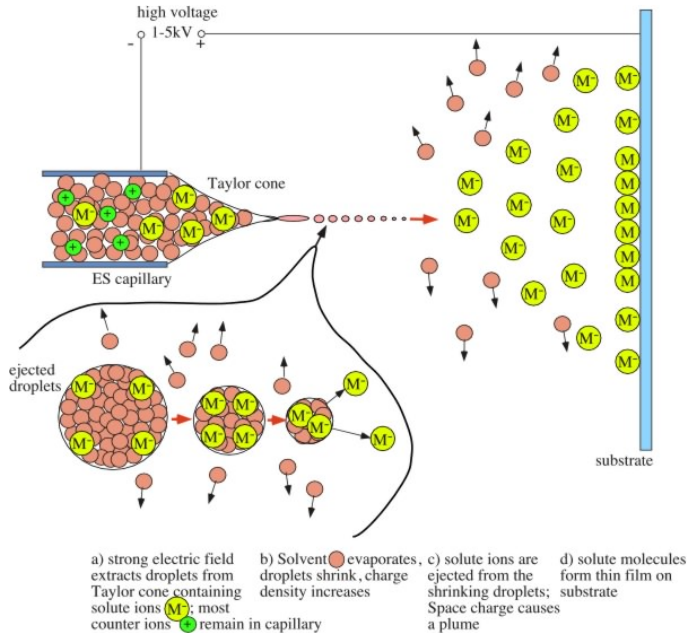
Close Coupled Showerhead

Date: P:  
26.07.2004:45

Thomas Swan  
Scientific Equipment

*RIXTRON*

# Electrospray deposition



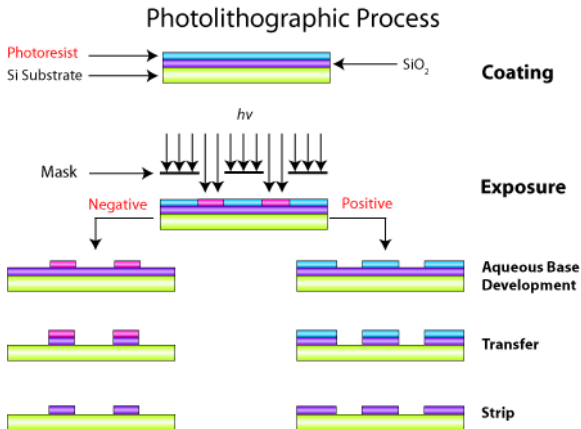
<http://rs1.eng.usf.edu/Pages/ResearchElectrosprayAmbient.html>

# Outline

- 1 Content
- 2 Relation between symmetry of crystals and crystal properties
- 3 Introduction
- 4 Bulk crystal growth
- 5 Thin film preparation
- 6 Lateral structures**
- 7 ATR / Surface plasma resonance

# Photolithography: top-down approach

- First, entire layered structure is grown. Then part of it is etched.
- Lateral limit given by optical resolution (can be overcome UV light, extreme UV, X-ray etc, sub-wavelength diffraction masks, immersion photolithography)
- Instead of mask and subsequent optical illumination, exposure can be done by e-beam.
- current lateral resolution cca 16 nm.



<http://withfriendship.com/user/levis/photolithography.php>



# Lithography: standard and lift-off process

Lift-off: mainly to have good metal/metal interface.

Advantages:

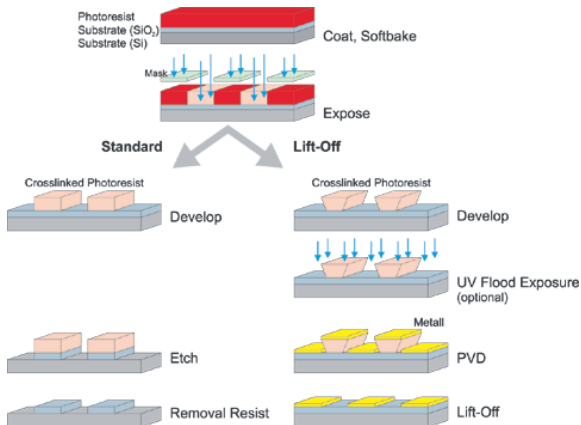
- do not need etching.

Disadvantages

- Retention: not all (usually metallic) layer is washed out and stays on the wafer.

- Ears: When the metal is deposited, and it covers the sidewalls of the resist, "ears" can be formed.

- Redeposition: it is possible that particles of metal will become reattached to the surface, at a random location.

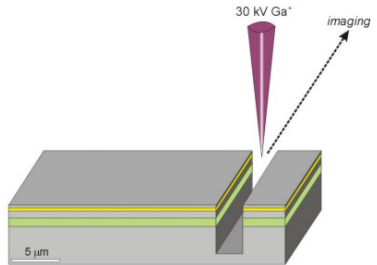


<http://www.microresist.de>

# Focused ion beam (FIB) nanofabrication

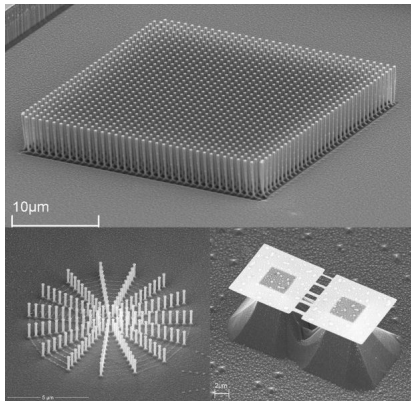
Focused ion beam (FIB):

- 1 source of ions (usually  $\text{Ga}^+$  or  $\text{He}^+$ )
- 2 beam optics (similar to scanning electron microscopy)
- 3 ions are focused to sample surface (focus diameter down to 1 nm)
- 4 local remove of atoms by ions (FIB-milling)

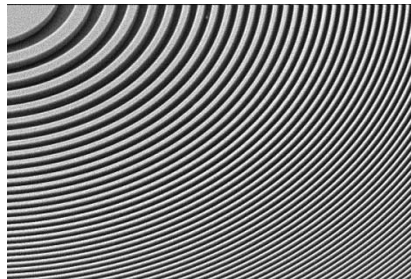


<http://web2.ges.gla.ac.uk/~mlee/FIBtec.htm>

# FIB nanostructures examples



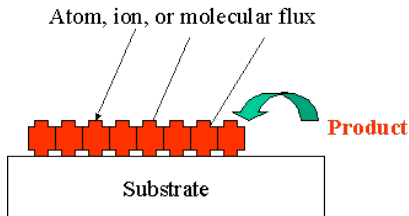
[http://nano.aalto.fi/en/research/groups/mqs/research/micro\\_and\\_nanofabrication/](http://nano.aalto.fi/en/research/groups/mqs/research/micro_and_nanofabrication/)



[www.raith.com](http://www.raith.com)

# Bottom-up approach

- The opposite of the top-down approach.
- Instead of taking material away to make structures, the bottom-up approach selectively adds atoms to create structures.



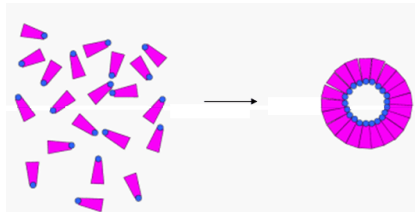
[http://idol.union.edu/~malekis/ESC24/KoskywebModules/sa\\_topd.htm](http://idol.union.edu/~malekis/ESC24/KoskywebModules/sa_topd.htm)

# The Ideas Behind the Bottom-up Approach

Nature uses the bottom up approach.

- Cells
- Crystals
- Humans

Chemistry and biology can help to assemble and control growth.



<http://www.csacs.mcgill.ca/selfassembly.htm>

# Why is Bottom-Up Processing Needed?

- Allows smaller geometries than photolithography.
- Certain structures such as Carbon Nanotubes and Si nanowires are grown through a bottom-up process.
- New technologies such as organic semiconductors employ bottom-up processes to pattern them.
- Can make formation of films and structures much easier.
- Is more economical than top-down in that it does not waste material to etching.

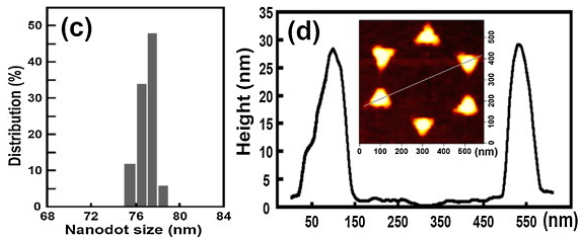
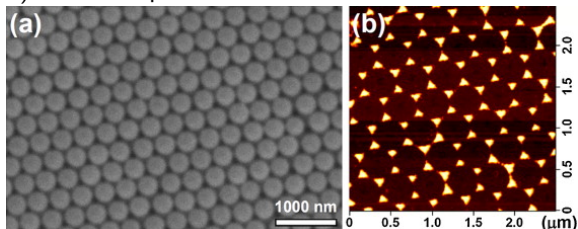
[http://courses.ee.psu.edu/ruzy11o/ee518/EE518\\_Top-down%20and%20Bottom-up1.ppt](http://courses.ee.psu.edu/ruzy11o/ee518/EE518_Top-down%20and%20Bottom-up1.ppt)

# Self Assembly

- The principle behind bottom-up processing.
- Self assembly is the coordinated action of independent entities to produce larger, ordered structures or achieve a desired shape.
- Found in nature.
- Start on the atomic scale.

# Example 1: self-assembled nanodots

- 1) Self-assembled monolayer of 340 nm-diameter polystyrene spheres
- 2) Ni film deposited and balls removed

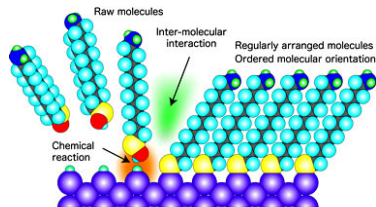


AppliedSurfaceScience257, 8712, (2011)



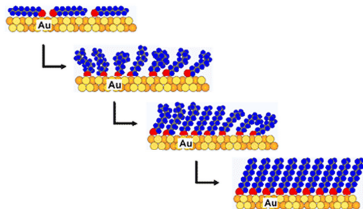
## Example 2: Self-assembled Monolayers (SAMS)

- Molecules are deposited molecule-by-molecule to form a self-assembled monolayer.
- Creates a high quality layers.
- Layers are deposited one layer at a time.
- Organic molecules can't be deposited using extreme conditions because it would damage the organic molecules.
- SAMS technique does not damage organic molecules.
- SAMS films are nearly defect free.
- Used to deposit organic semiconductors.



Substrate (metals, semiconductors, ceramics, polymers, etc.)

<http://www.mtl.kyoto-u.ac.jp/english/laboratory/nanoscopic/nanoscopic.htm>



<http://www.seas.upenn.edu/>

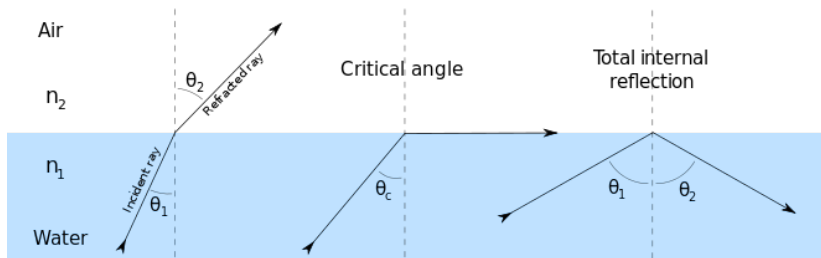
# Other examples of self assembly

- carbon nanotubes
- ...

# Outline

- 1 Content
- 2 Relation between symmetry of crystals and crystal properties
- 3 Introduction
- 4 Bulk crystal growth
- 5 Thin film preparation
- 6 Lateral structures
- 7 ATR / Surface plasma resonance

# Reflection and total reflection



Snell law:

$$\sqrt{\epsilon_1} \sin \varphi_1 = \sqrt{\epsilon_2} \sin \varphi_2$$

Critical angle:

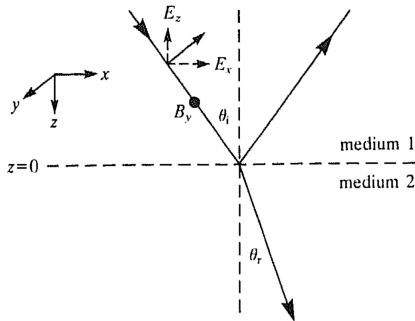
$$\sin \varphi_c = \sqrt{\frac{\epsilon_2}{\epsilon_1}}$$

# Light reflection on the interface

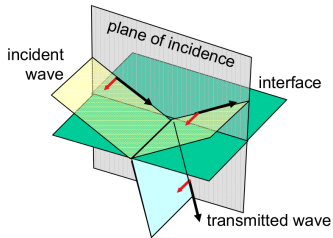
- 1 Maxwell equations
- 2 solution as plane wave  

$$E = E_0 \exp(i(\vec{k} \cdot \vec{r} - \omega t))$$
- 3 boundary conditions at the interface:  
 $\vec{E}, \vec{H}$  fields: continuous transverse ( $x, y$ ) components  
 $\vec{D}, \vec{B}$  fields: continuous normal ( $z$ ) components
- 4 for total reflection, solution of transverse wave is in form so called evanescent wave, non-propagating in  $z$ -direction  

$$E = E \exp(-k_z z)$$



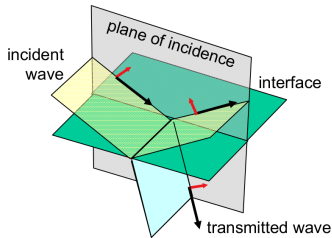
# Light reflection on the interface



s-polarized light:

$$r_{\perp} = \frac{n_i \cos(\theta_i) - n_t \cos(\theta_t)}{n_i \cos(\theta_i) + n_t \cos(\theta_t)}$$

$$t_{\perp} = \frac{2n_i \cos(\theta_i)}{n_i \cos(\theta_i) + n_t \cos(\theta_t)}$$



p-polarized light:

$$r_{\parallel} = \frac{n_i \cos(\theta_t) - n_t \cos(\theta_i)}{n_i \cos(\theta_t) + n_t \cos(\theta_i)}$$

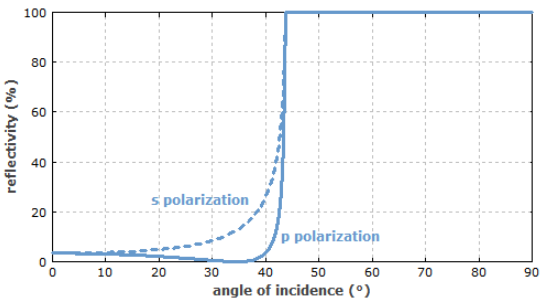
$$t_{\parallel} = \frac{2n_i \cos(\theta_i)}{n_i \cos(\theta_t) + n_t \cos(\theta_i)}$$

And, for both polarizations:  $n_i \sin(\theta_i) = n_t \sin(\theta_t)$

<http://www.ece.rice.edu/~daniel/262/pdf/lecture14.pdf>

# Light reflection on the interface

## Reflection on glass/air



# Total reflection

Critical angle:

$$\sin \varphi_c = \sqrt{\frac{\varepsilon_2}{\varepsilon_1}} = \frac{n_2}{n_1}$$

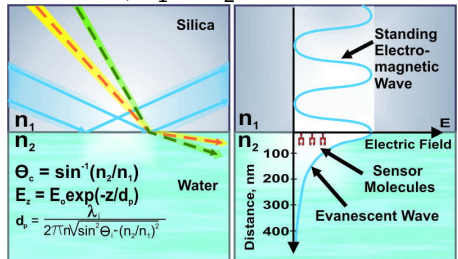
Evanescent wave:

$$E = E_t \exp(-z/\delta - i\omega t)$$

Penetration depth:

$$\delta = \frac{1}{k_0 \sqrt{(n_1 \sin \varphi_1)^2 - (n_2^2)}}$$

Example: glass( $n_1$ )/water( $n_2$ )  
interface;  $n_1 > n_2$



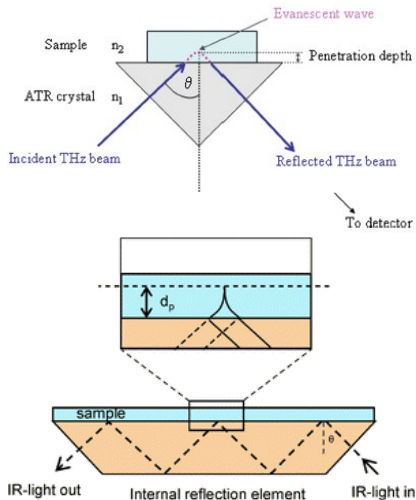
<http://www.tirftechnologies.com/principles.php>



# Attenuated total reflectance (ATR)

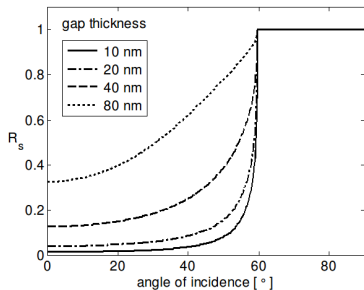
(Zeslabený úplný odraz)

- probes sample by evanescent wave
- ⇒ sensitive to surface of the sample
- sample modifies evanescent wave → partial absorption or transmission of light in sample → total reflection is decreased (attenuated).
- reflected beam does not follow exactly geometrical optics → The Goos-Hänchen shift

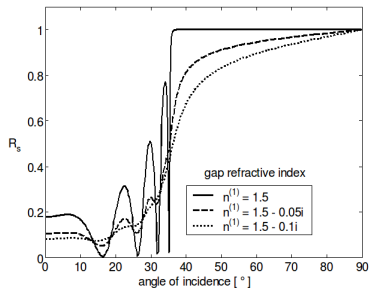


# Attenuated total reflectance (ATR): gap effect

Gap thickness (refractivity of gap=1):



Absorption in gap (gap thickness 960 nm):



# Surface plasmon I: derivation

Electric field in the vicinity of the interface:

$$E = E_0 \exp[i(k_x x + k_z z - \omega t)]$$

where

$$k^2 = k_x^2 + k_z^2 = \epsilon (\omega/c)^2 = \epsilon k_0^2 \quad (1)$$

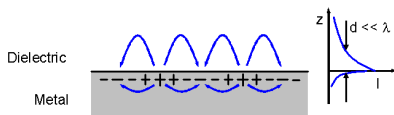
At the interface of two materials  $\epsilon_1$  and  $\epsilon_2$ :

(a)  $k_x$  continuous over the interface;

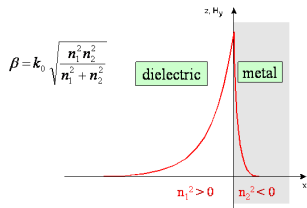
$$k_{x1} = k_{x2} \quad (2)$$

(b)  $D_z$  and  $E_x$  continuous over the interface

$$k_{z1}/\epsilon_1 = k_{z2}/\epsilon_2 \quad (3)$$



## Surface Plasmon Resonance



Note! There is only a single p-polarized (TM) surface plasmon !

<http://www.physics.uwo.ca/~smittler/>

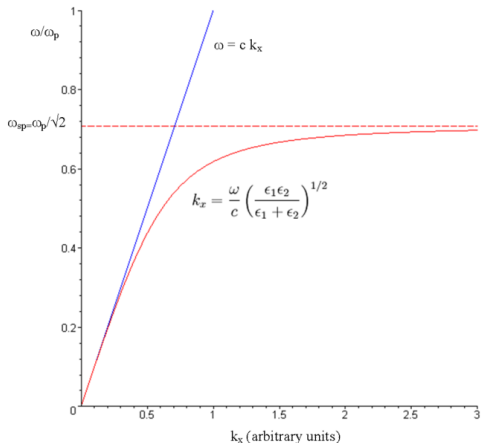
# Surface plasmon II: dispersion relation

- From Eqs.(1-3) follows dispersion relation for surface plasmon:

$$k_x = k_0 \sqrt{\left( \frac{\epsilon_1 \epsilon_2}{\epsilon_1 + \epsilon_2} \right)}, \quad (4)$$

where  $k_0 = \omega/c$ .

- Surface plasmon appears only for p-polarized (TM) wave, as this mode has normal (z) component of  $D = \epsilon \epsilon_0 E$  field.



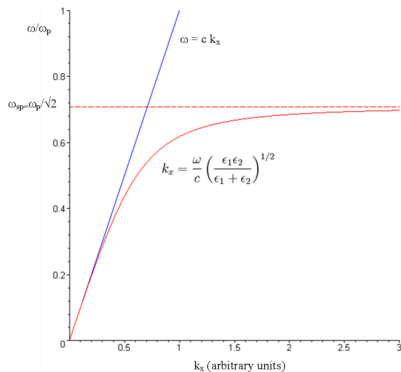
# Surface plasmon III: example

Example: assuming  $\epsilon_1 = 1$  (air) and  $\epsilon_2 = 1 - \frac{\omega_p^2}{\omega^2}$  (metal as free electron model of an electron gas). Then

$$k_x = \frac{\omega}{c} \sqrt{\left( \frac{\omega^2 - \omega_p^2}{2\omega^2 - \omega_p^2} \right)} \quad (5)$$

Hybridization between photon ( $\omega = ck_0$ ) and plasmon

$$\omega_{SP} = \omega_p / \sqrt{2}.$$



# Surface plasma resonance (SPR) I

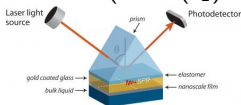
- Resonance between incident wave photon and surface plasmon. Resonance means that both (pseudo)-particles have equal  $\omega$  and  $k_x = k_{x,inc} = \Re(k_{x,sp})$ .
- Description of incident wave from material  $\epsilon_1$  under angle  $\varphi$ :

$$k_{x,inc} = \frac{\omega}{c} \sqrt{\epsilon_1} \sin \varphi \quad (6)$$

- Description of surface plasmon:

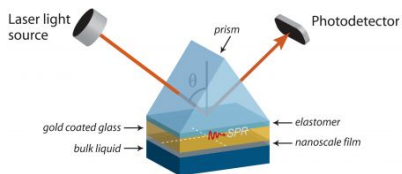
$$k_{x,sp} = \left(\frac{\omega}{c}\right) \sqrt{\left(\frac{\epsilon_1 \epsilon_2}{\epsilon_1 + \epsilon_2}\right)}, \quad (7)$$

Condition for existence of the resonance:  $\Re(\epsilon_2) < -\epsilon_1$  (i.e.  $\Re(\epsilon_2)$  must be negative; fulfilled by coinage metals, Au, Ag, Cu). Here,  $\epsilon_1$  is assumed to be non-absorbing material (i.e.  $\Im(\epsilon_1) = 0$ ).



# Surface plasma resonance (SPR) II

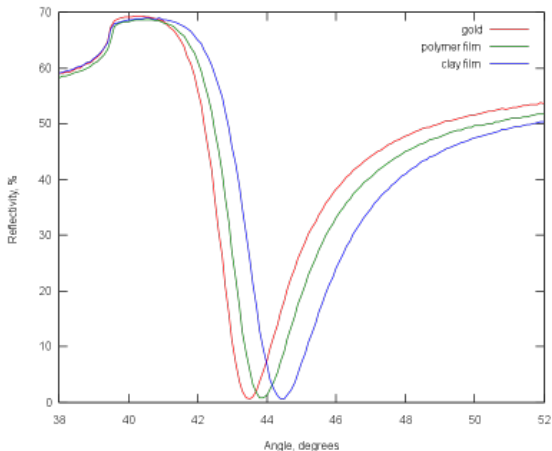
Surface plasmons are very sensitive to slight perturbations within the skin depth  $\Rightarrow$  surface plasmons are often used to probe tiny changes of refraction index near the interface (extreme sensitive detector of small changes of the refraction index).  
 $\Rightarrow$  Readout of many bio-sensors based on this detection technique.



<http://www.bionavis.com/technology/spr/>

# SPR: detection I

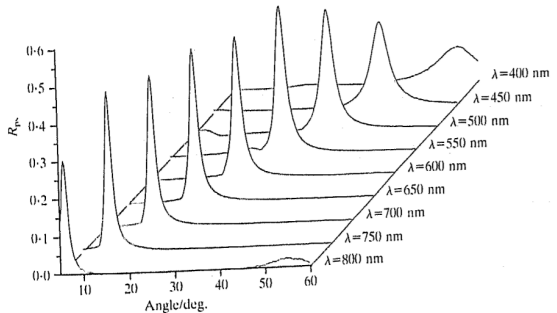
- presence of resonance increases absorption and reduces reflectivity.
- position of reflection minima very sensitive to refractivity index in position of the evanescent wave.





# SPR: detection II

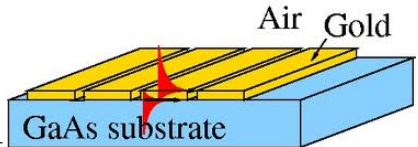
- presence of resonance increases absorption and reduces reflectivity.
- position of reflection minima very sensitive to refractivity index in position of the evanescent wave.



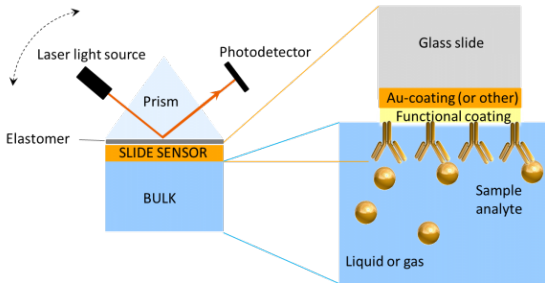
# SPR: how to couple surface plasmon and photon?

- couple light by high-refraction index prism
- lateral modulation of the interface (roughness or structuring)

$$\omega/c \sin \varphi + 2\pi/b = \omega/c \sqrt{\frac{\epsilon_2}{\epsilon_2 + 1}} \quad (8)$$



# SPR: bio sensors



<http://www.bionavis.com/technology/spr/>